



CHAPTER 5 TRIGONOMETRIC RATIOS

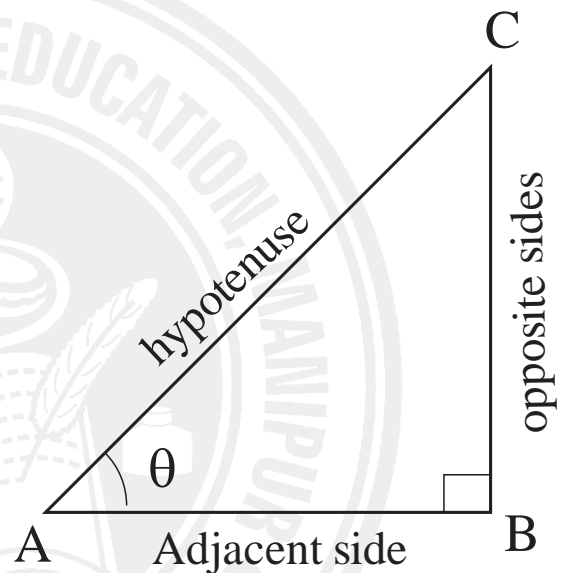
NOTES

TRIGONOMETRIC RATIOS:

The ratios of the sides of a right triangle with respect to its acute angles are called trigonometric ratios of angles. There are six such trigonometric ratios. They are sine, cosine, tangent, cosecant, secant and cotangent of an angle θ . In short, they are written as $\sin \theta$, $\cos \theta$, $\tan \theta$, $\operatorname{cosec} \theta$, $\sec \theta$ and $\cot \theta$ respectively.

We have,

$$\sin \theta = \frac{BC}{AC} = \frac{\text{opp.}}{\text{hypo.}}$$
$$\cos \theta = \frac{AB}{AC} = \frac{\text{adj.}}{\text{hypo.}}$$
$$\tan \theta = \frac{BC}{AB} = \frac{\text{opp.}}{\text{Adj.}}$$
$$\cot \theta = \frac{AB}{BC} = \frac{\text{adj.}}{\text{opp.}}$$
$$\sec \theta = \frac{AC}{AB} = \frac{\text{hypo.}}{\text{adj.}}$$
$$\operatorname{cosec} \theta = \frac{AC}{BC} = \frac{\text{hypo.}}{\text{opp.}}$$



RECIPROCAL RELATIONS:

1. $\sin \theta = \frac{1}{\operatorname{cosec} \theta}$
2. $\cos \theta = \frac{1}{\sec \theta}$
3. $\tan \theta = \frac{1}{\cot \theta}$

1. THREE IDENTITIES:

- (i) $\sin^2 \theta + \cos^2 \theta = 1$
- (ii) $1 + \tan^2 \theta = \sec^2 \theta$
- (iii) $1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$





2. QUOTIENT RELATIONS:

(i) $\tan \theta = \frac{\sin \theta}{\cos \theta}$

(ii) $\cot \theta = \frac{\cos \theta}{\sin \theta}$

